# High image resolution NASA CALIOP extinction denoising / inference

**Constructive insights for future space-based missions** 

Willem J. Marais, Robert E. Holz, Mark A. Vaughan, Charles R. Trepte, John W. Hair, Chris A. Hostetler

12/04/2023



### Langley NASA CALIOP

1.0x10<sup>-1</sup> 9.0 8.0 7.0 6.0 5.0 4.0 3.0 2.0 1.0x10<sup>-2</sup> 8.0 7.5 7.0 6.5 6.0 5.5 5.0 4.5 4.0 3.5 3.0 2.5 2.0 1.5 1.0x10<sup>-3</sup> 9.0 8.0 7.0 6.0 5.0 4.0 3.0 2.0 1.0x10<sup>-4</sup>



### Langley NASA CALIOP

1.0x10<sup>-1</sup> 9.0 8.0 7.0 6.0 5.0 4.0 3.0 2.0 1.0x10<sup>-2</sup> 8.0 7.5 7.0 6.5 6.0 5.5 5.0 4.5 4.0 3.5 3.0 2.5 2.0 1.5 1.0x10<sup>-3</sup> 9.0 8.0 7.0 6.0 5.0 4.0 3.0 2.0 1.0x10<sup>-4</sup>

![](_page_3_Figure_0.jpeg)

### Denoised total attenuated backscatter (Horizontal 1km, Vertical 60m) 8 2016-08-10 (nighttime) 6 Altitude (km) 2

38 39

![](_page_4_Picture_2.jpeg)

![](_page_4_Picture_4.jpeg)

- CALIOP noisy image: y
- Attenuated scattering ratio: *x*
- CALIOP forward model: F(x)
- CALIOP noise model:  $\ell(y | F(x))$
- A priori assumption about attenuated scattering ratio: p(x)

- CALIOP noisy image: y
- Attenuated scattering ratio: *x*
- CALIOP forward model: F(x)
- CALIOP noise model:  $\ell(y | F(x))$
- A priori assumption about attenuated scattering ratio: p(x)

The raw level-0 digitizer counts

- CALIOP noisy image: y
- Attenuated scattering ratio: x
- CALIOP forward model: F(x)
- CALIOP noise model:  $\ell(y | F(x))$
- A priori assumption about attenuated scattering ratio: p(x)

- The raw level-0 digitizer counts
- -• Estimate parl. & perp. separately

- CALIOP noisy image: y
- Attenuated scattering ratio: *x*
- CALIOP forward model: F(x)
- CALIOP noise model:  $\ell(y | F(x))$
- A priori assumption about attenuated scattering ratio: p(x)

- The raw level-0 digitizer counts
- Estimate parl. & perp. separately
- Model expected value of y

- CALIOP noisy image: y
- Attenuated scattering ratio: *x*
- CALIOP forward model: F(x)
- CALIOP noise model:  $\ell(y | F(x))$
- A priori assumption about attenuated scattering ratio: p(x)

- The raw level-0 digitizer counts
- Estimate parl. & perp. separately
- Model expected value of y
- Model noise statistical properties

### The noise model **Spatially-varying and signal-dependent noise variance**

![](_page_10_Figure_1.jpeg)

# **CALIOP** noise probability distribution

![](_page_11_Figure_1.jpeg)

### **Starting with something familiar** The formulation of optimal estimation

- CALIOP noisy image: y
- Attenuated scattering ratio: *x*
- CALIOP forward model: F(x)
- CALIOP noise model:  $\ell(y | F(x))$
- A priori assumption about attenuated scattering ratio:  $p(x)^{\bullet}$

- The raw level-0 digitizer counts
- Estimate parl. & perp. separately
- Model expected value of y
- Model noise statistical properties

 Promote structure / spatial + temporal correlation in image

### **Poisson total variation (PTV) PTV** approximates the image as piecewise constant

![](_page_13_Picture_1.jpeg)

### cross-section

![](_page_13_Figure_3.jpeg)

Willem J. Marais, et. al., "Approach to simultaneously denoise and invert backscatter and extinction from photon-limited atmospheric lidar observations" (2016)

![](_page_13_Picture_5.jpeg)

### Patch based denoising Exploit redundancy in image that allows for accurate approximation of a richer class of images

![](_page_14_Picture_2.jpeg)

![](_page_14_Picture_3.jpeg)

Marais, Willem, and Rebecca Willett. "Proximal-gradient methods for Poisson image reconstruction with bm3d-based regularization." In 2017 IEEE 7th International Workshop on Computational Advances in Multi-Sensor Adaptive Processing (CAMSAP), pp. 1-5. IEEE, 2017.

![](_page_15_Figure_0.jpeg)

![](_page_15_Figure_1.jpeg)

![](_page_16_Figure_0.jpeg)

1]
SL
 -
Ę
;
tte
sca
Š
þa
ed
uat
eni
att
Ð
La
рa

![](_page_17_Figure_0.jpeg)

![](_page_17_Picture_2.jpeg)

S

### Denoised total attenuated backscatter (Horizontal 1km, Vertical 60m) 8 2016-08-10 (nighttime) 6 Altitude (km) 2

38 39

![](_page_18_Picture_2.jpeg)

![](_page_18_Picture_4.jpeg)

![](_page_19_Figure_0.jpeg)

total attenuated backscatter [1/km 1/sr]

![](_page_19_Picture_3.jpeg)

### **Profile A - 37.29°**

![](_page_20_Figure_1.jpeg)

### Profile B - 40.37°

![](_page_21_Figure_1.jpeg)

![](_page_23_Picture_1.jpeg)

### **Cross-validation: Choosing the regularization parameter Step 1: Holdout pixels**

![](_page_24_Figure_1.jpeg)

**CALIOP** noisy image

# holdout pixels

# holdout pixels

![](_page_24_Figure_5.jpeg)

![](_page_24_Figure_6.jpeg)

### **Cross-validation: Choosing the regularization parameter** Step 2: Denoise and interpolate over holdout pixels 2) Choose estimate with 1) For regularization parameter $\lambda$ denoise regularization parameter $\lambda$ which best fits holdout pixels & interpolate

![](_page_25_Figure_1.jpeg)

CALIOP parallel backscatter digitizer counts from 2016-09-18 13:34:

![](_page_25_Picture_3.jpeg)

### The three keys ideas that OE shares with regularized maximum likelihood estimation

**Noise model quantifies** goodness of fit between F(x) and y

# 2) Regularizer function that promotes a priori about x $\ell(y \mid F(x)) + \lambda p(x)$

3) Regularization parameter sets the degree to which the a priori of x is promoted

### **Error vs the regularization parameter** Intuition behind the regularization parameter

![](_page_27_Figure_1.jpeg)

![](_page_27_Picture_2.jpeg)

High bias (e.g. smoothing)  $\tilde{p}_g(x)$  Low variance

### $\lambda$ - regularization parameter

![](_page_27_Picture_5.jpeg)

![](_page_28_Figure_0.jpeg)

Time [UTC]

Willem J. Marais, et. al., "Approach to simultaneously denoise and invert backscatter and extinction from photon-limited atmospheric lidar observations" (2016)

![](_page_28_Picture_4.jpeg)

### **Denoising UW High Spectral Resolution Lidar data** 10<sup>-4</sup> 7000 7000 6000 lidar ratio [sr] **PTV** backscatter [m<sup>-1</sup> sr<sup>-1</sup>] 6000 ection [m (Poisson total ے ج 10<sup>-5</sup> <u>5000 ا</u> variation) Altitude 3000 Altitude 9000 Altitude Cross-s $10^{-6}$ ackscatter 2000 2000 1000 1000 10-02:00 05:00 06:00 01:00 03:00 00:00 04:00 02:01 07:00 HSRL total column AOD with 0.08 AOD offset n aerosol optical depth 0.5 Time [UTC] AERONET AOD 0.4 0.3 0.2 Colum 0.1 02:00 03:00 06:00 07:00 05:00 04:00 07:00 Willem J. Marais, et. al., "Approach to simultaneously denoise and invert Time [UTC]

![](_page_29_Figure_1.jpeg)

![](_page_29_Figure_2.jpeg)

# **Denoising NCAR Micro Pulse DIAL (MPD) data**

![](_page_30_Figure_1.jpeg)

![](_page_30_Figure_2.jpeg)

Willem J. Marais, and Matthew Hayman. "Extending water vapor measurement capability of photon limited differential absorption lidars through simultaneous denoising and inversion." Atmospheric Measurement Techniques (2022)